

**Μπορείτε να πάρετε οποιαδήποτε άσκηση ή πρόβλημα από το υλικό του 1<sup>ου</sup> εξαμήνου και να το λύσετε με μετασχηματισμό Laplace: το αποτέλεσμα πρέπει να βγει ίδιο!**

## ΕΠΠΡΟΣΘΕΤΑ ΠΡΟΒΛΗΜΑΤΑ ΜΕ ΤΕΛΙΚΗ ΑΠΑΝΤΗΣΗ

**P 14.8-1** Using Laplace transforms, find the response  $i_L(t)$  for  $t > 0$  for the circuit of Figure P 14.8-1.

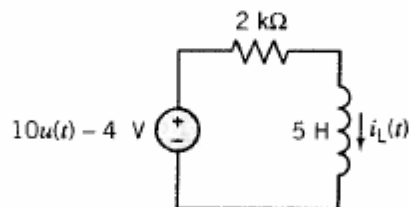


Figure P 14.8-1

$$i_L(t) = \begin{cases} -2 \text{ mA} & t < 0 \\ 3 - 5e^{-400t} \text{ mA} & t > 0 \end{cases}$$

**P 14.8-2** Using Laplace transforms, find the response  $i_L(t)$  for  $t > 0$  for the circuit of Figure P 14.8-2.

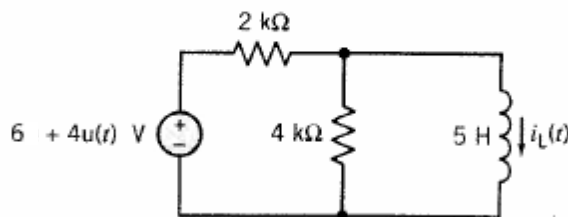


Figure P 14.8-2

$$i_L(t) = 5 - 2e^{-\frac{4000}{15}t} \text{ mA}, t > 0$$

**P 14.8-3** Using Laplace transforms, find the response  $v_c(t)$  for  $t > 0$  for the circuit of Figure P 14.8-3.

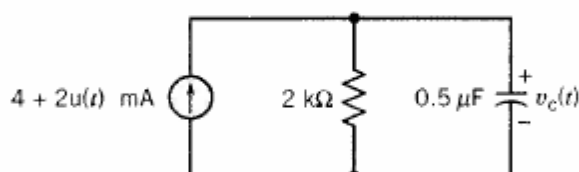


Figure P 14.8-3

$$V_c(t) = 12 - 4e^{-1000t} \text{ V}, t > 0$$

**P 14.8-4** Using Laplace transforms, find the response  $v_c(t)$  for  $t > 0$  for the circuit of Figure P 14.8-4.

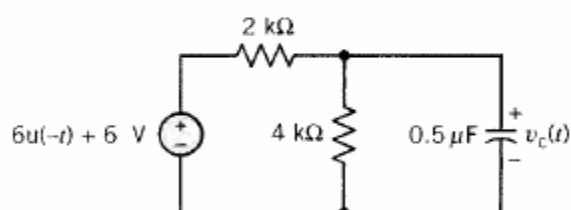


Figure P 14.8-4

$$v_c(t) = 4 + 4e^{-1500t} \text{ V}, t > 0$$

**P 14.8-5** Using Laplace transforms, find the response  $v(t)$  for  $t > 0$  for the circuit of Figure P 14.8-5 when  $v_s = 6e^{-3t}u(t)$  V.  
**Answer:**  $v = \frac{44}{3}e^{-2t} + \frac{1}{3}e^{-5t} - 9e^{-3t}$  V

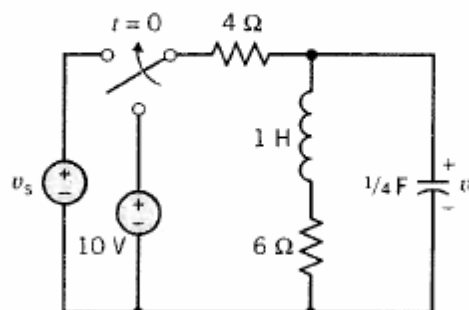
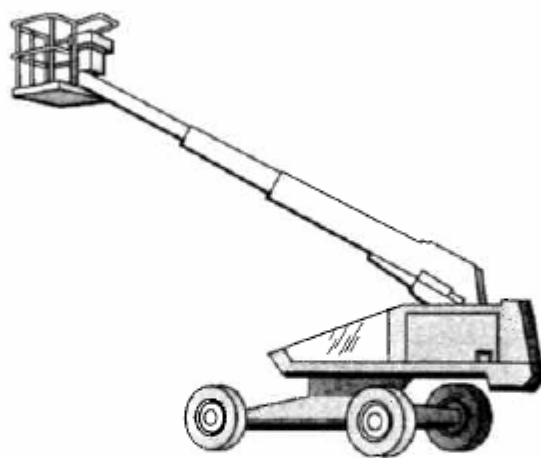


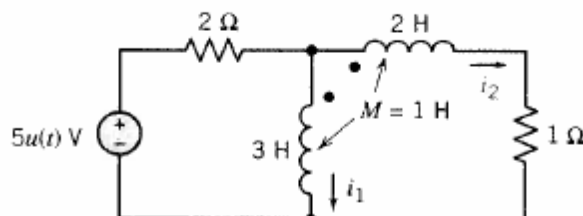
Figure P 14.8-5

$$v_c(t) = 44/3 e^{-2t} - 9e^{-3t} + (1/3)e^{-5t} \text{ V}$$

**P 14.8-7** The motor circuit for driving the snorkel shown in Figure P 14.8-7a is shown in Figure P 14.8-7b. Find the motor current  $i_2(s)$  when the initial conditions are  $i_1(0^-) = 2$  A and  $i_2(0^-) = 3$  A. Determine  $i_2(t)$  and sketch it for 10 seconds. Does the motor current smoothly drive the snorkel?



(a)



(b)

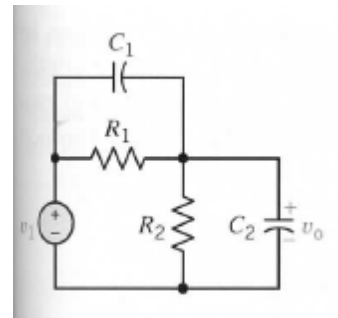
Figure P 14.8-7 Motor drive circuit for snorkel device.

$$i_2(t) = 0.64e^{-0.26t} + 2.36e^{-1.54t} \text{ A for } t > 0$$

## ΠΙΟ ΠΡΟΧΩΡΗΜΕΝΑ ΠΡΟΒΛΗΜΑΤΑ

**P 14.9-1** Consider the circuit of Figure P 14.9-1, where the combination of  $R_2$  and  $C_2$  represents the input of an oscilloscope. The combination of  $R_1$  and  $C_1$  is added to the probe of the oscilloscope to shape the response  $v_0(t)$  so that it will equal  $v_1(t)$  as closely as possible. Find the necessary relationship for the resistors and capacitors so that  $v_0 = av_1$  where  $a$  is a constant.

**Hint:** Find the transfer function  $V_0(s)/V_1(s)$ . Choose  $R_1$  and  $C_1$  so that the transfer function does not depend on  $s$ .



$$R_1 C_1 = R_2 C_2$$

**P 14.9-2** Consider the circuit shown in Figure P 14.9-2. Show that by proper choice of  $L$ , the input impedance  $Z = V_1(s)/I_1(s)$  can be made independent of  $s$ . What value of  $L$  satisfies this condition? What is the value of  $Z$  when it is independent of  $s$ ?

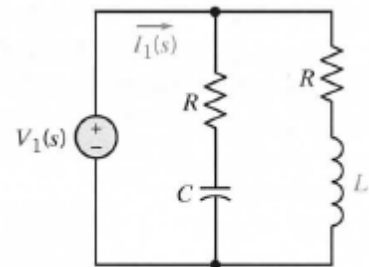


Figure P 14.9-2

$$L = R^2 C \quad \text{then} \quad Z = R$$

**P 14.9-3** A bridged-T circuit is often used as a filter and is shown in Figure P 14.9-3. Show that the transfer function of the circuit is

$$\frac{V_{\text{out}}(s)}{V_{\text{in}}(s)} = \frac{1 + (2R_1 + R_2)Cs + R_1 R_2 C^2 s^2}{1 + 2R_1 Cs + R_1 R_2 C^2 s^2}$$

